RNA Bioinformatics

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- ▶ PART 1: RNA Structures and How to Compute Them
- PART 2: RNA Landscapes
- PART 3: The Modern RNA World

PART1

Why RNA?

- until relatively recently:
 - Central Dogma of Molecular Biology
 - $\mathsf{DNA} \to \mathsf{RNA} \to \mathsf{Protein}$
 - $\mathsf{DNA}=$ "genetic memory", $\mathsf{RNA}=\mathsf{working}$ copy, proteins do the work
- around 1980: discovery of catalytic RNAs (Nobelprize for Tom Cech and Sidney Altman) nevertheless long considered "exotic" remnants from the ancient RNA world
- around 2000: structure of the ribosome showns that the ribosome is an "RNA enzyme"
- around 2000: microRNAs are discovered as a large class of regulatory RNAs that inhibit translation of proteins
- 2006: the ENCODE project shows that human gene expression is quite different from textbook knowledge

RNA Bioinformatics

RNA Secondary Structures are an appropriate level of description

- explain the thermodynamics of RNA Structures
- often highly conserved in evolution
- can be computed efficiently

Many Functional RNAs are Structured



- (a) Group I intron P4-P6 domain
- (b) Hammerhead ribozyme
- (c) HDV ribozyme
- (d) Yeast tRNA $^{\rm phe}$
- (e) L1 domain of 23S rRNA

Hermann & Patel, JMB 294, 1999

The RNA Model



Formal Definition

A secondary structure on a sequence s is a collection of pairs (i, j) with i < j such that

- ► Base pairing rules are respected, i.e., $(i, j) \in \Omega$ implies (s_i, s_j) form an allowed pair (GC, CG, AU, UA, GU, UG)
- Each base is involved in at most one pair, i.e., Ω is a matching, (i, j), (i, k) ∈ Ω implies j = k and (i, k), (j, k) ∈ Ω in implies i = j.
- $(i,j)\Omega$ implies |j-i| > 3 (sterical constraint)
- No-crossing rule: (i, j), (k, l) ∈ Ω and i < k implies either i < k < l < j or i < j < k < l.</p>
 This evaluates as called records/mate.

This excludes so-called pseudoknots

Let's count the structures . . .

Counting secondary structures. Given a sequence of length *n*. $\Pi_{kl} = 1$ if sequence positions *k*, *l* can form a pair GC, CG, AU, UA, GU, UG and $\Pi_{kl} = 0$ otherwise. N_{kl} = number of structures of the *subsequence* from *k* to *l*. Basic recursion:

•
$$xxxxxxx + \sum (xxxx)xxxx$$

$$N_{kl} = N_{k+1,l} + \sum_{j=k+m}^{l} \prod_{kj} N_{k+1,j-1} N_{j+1,l}$$

RNA Folding in a nutshell



$$N_{ij} = N_{i+1,j} + \sum_{\substack{k \\ (i,k) \text{pair}}}^{k} N_{i+1,k-1} N_{k+1,j}$$

$$E_{ij} = \min \left\{ E_{i+1,j} + \min_{\substack{k \\ (i,k) \text{pair}}}^{k} (E_{i+1,k-1} + E_{k+1,j} + \varepsilon_{ik}) \right\}$$

$$Z_{ij} = Z_{i+1,j} + \sum_{\substack{k \\ (i,k) \text{pair}}}^{k} Z_{i+1,k-1} Z_{k+1,j} \exp(-\varepsilon_{ik}/RT)$$

Partition function: $Z = \sum_{\Omega} \exp(-E(\Omega)/RT)$

A word on the Partition Function

The partition function is the link between the combinatorics of the structures (in general: states in an ensemble) and the thermodynamic properties of the physical ensemble, e.g.:

Free energy
$$G = -RT \ln Z$$

• Expected Energy
$$\langle E \rangle = RT^2 \frac{\partial \ln Z}{\partial T}$$

• Heat Capacity $C_p = -T \frac{\partial^2 G}{\partial T^2}$



Realistic Energy Model



Parameters from large number of melting experiments by Douglas Turner, David Matthews, John Santa Lucia, and others

Recursions for Linear RNAs



Recursions for Linear RNAs

- F_{ij} free energy of the optimal substructure on the subsequence x[i, j].
- C_{ij} free energy of the optimal substructure on the subsequence x[i,j] subject to the constraint that i and j form a base pair.
- M_{ij} free energy of the optimal substructure on the subsequence x[i,j] subject to the constraint that that x[i,j] is part of a multiloop and has at least one component, i.e., a sub-sequence that is enclosed by a base pair.
- M_{ij}^1 free energy of the optimal substructure on the subsequence x[i,j] subject to the constraint that that x[i,j] is part of a multiloop and has exactly one component, which has the closing pair i, h for some h satisfying $i \le h < j$.

Recursions for Linear RNAs

$$F_{ij} = \min \left\{ F_{i+1,j}, \min_{i < k \le j} C_{ik} + F_{k+1,j} \right\}$$

$$C_{ij} = \min \left\{ \mathcal{H}(i,j), \min_{i < k < l < j} C_{kl} + \mathcal{I}(i,j;k,l), \right.$$

$$\min_{i < u < j} M_{i+1,u} + M_{u+1,j-1}^{1} + a \right\}$$

$$M_{ij} = \min \left\{ \min_{i < u < j} (u - i - 1)c + C_{u+1,j} + b, \right.$$

$$\min_{i < u < j} M_{i,u} + C_{u+1,j} + b, M_{i,j-1} + c \right\}$$

$$M_{ij}^{1} = \min \left\{ M_{i,j-1}^{1} + c, C_{ij} + b \right\}$$

Backward Recursion: Base Pairing Probabilities

$$p_{ij} = rac{Z_{1,i-1}\widehat{Z}_{i,j}Z_{j+1,n}}{Z_{1,n}} + \sum_{k < i} \sum_{l > j} p_{kl} \Xi_{ij,kl} \,.$$

$$\begin{split} &\Xi_{ij,kl} \text{ is a ratio of the two partition functions:} \\ &\widehat{Z}_{ij,kl} \dots \text{ both } i,j \text{ and } k,l \text{ pair} \\ &\widehat{Z}_{kl} \dots k,l \text{ pair.} \\ &\text{Simplest case:} \\ &\widehat{Z}_{ij,kl} = Z_{k+1,i-1} \widehat{Z}_{ij} Z_{j+1,l-1} \zeta_{kl} \text{ where } \zeta_{kl} = \exp(-\beta_{kl}/RT) \text{ is the} \\ &\text{Boltzman factor of the pairing energy} \end{split}$$

Backward recursion: full model

Backward recursion:

$$P_{kl} = P_{kl}^{\circ} + \sum_{p < k;q > l} P_{pq} \frac{Z_{k,l}^{B}}{Z_{p,q}^{B}} \Biggl\{ e^{-\mathcal{I}(p,q,k,l)} + \Biggl(\sum_{p < u < k} Z_{p+1,u}^{M} Z_{u+1,k-1}^{M1}) \Biggr) e^{-(a+(q-l-1)c)} + \Biggl(\sum_{l < u < q} Z_{l+1,u}^{M} Z_{v+1,q-1}^{M1}) \Biggr) e^{-(a+(k-p-1)c)} + Z_{p+1,k-1}^{M} Z_{l+1,q-1}^{M} \Biggr\}$$

Single-Stranded Circular RNAs

- Viroid RNA
- Hepatitis Delta Virus Genome
- Cryptic by-products of splicing formed intronic sequence
- Circularized C/D box snoRNAs were recently reported in Pyrococcus furiosus
- Synthetic constructs for *in vitro* selection

Circular, Linear, and Interacting RNAs

In the maximum matching case \implies same algorithm for all three cases







CIRCULAR FOLDING

LINEAR FOLDING

BINARY COFOLDING

Linear versus Circular Folding

Linear folding: energy contributions *inside* a pair (i, j) only. Co-folding: additional contribution for loop spanning [n, 1].



Strategy 1 (e.g. Michael Zucker's mfold)

For each pair (i, j): compute energy both inside and outside the pair

- \Rightarrow doubles memory requirements
- Strategy 2 (Vienna RNA Package)
 First compute linear folding energies. Then compute energies for the loop spanning [n, 1].



Implementing Circular Folding

Relative to linear folding, only the loop containing the cut has to be re-evaluated.

Three cases: cut in Hairpin, Interior-, or Multi-loop

 $F^{\circ} = \min\{F_{H}^{\circ}, F_{I}^{\circ}, F_{M}^{\circ}\}$



Exterior Hairpin.

$$F_{H}^{\circ} = \min_{p < q} \left\{ C_{pq} + \mathcal{H}(q, p) \right\}$$

Exterior Interior Loop.

$$F_l^\circ = \min_{k < l < p < q} \{C_{pq} + C_{kl} + \mathcal{I}(q, p, l, k)\}$$

Exterior Multi-Loop.

Modified decomposition: one or more components $M_{1,k}$ + exactly two components $M_{k+1,n}^2$

$$M_{kn}^{2} = \min_{k < u < n} \left(M_{ku}^{1} + M_{u+1,n}^{1} \right)$$
$$F_{M}^{\circ} = \min_{1 < k < n} \left\{ M_{1,k} + M_{k+1,n}^{2} + a \right\}$$

• Folding energy: $F^{\circ} = \min\{F^{\circ}_{H}, F^{\circ}_{I}, F^{\circ}_{M}\}$



Applications of Circular Folding

Local structures

Idea: Restrict Recursion to base pairs (i, j) with j - i < L. Special interest in robust structures: $Z_{ij}^{u,L}$... partition function of sub-sequence [i, j] when sequence window [u, u + L] is folded $p_{ij}^{u,L}$... probability that i and j form a base pair when window [u, u + L] is folded.

$$\begin{split} Z_{ij}^{u,L} &= \begin{cases} Z_{ij} & \text{if } [i,j] \subseteq [u,u+L] \\ 0 & \text{otherwise} \end{cases} \\ p_{ij}^{u,L} &= \frac{Z_{1,i-1}^{u,L} \widehat{Z}_{i,j}^{u,L} Z_{j+1,n}^{u,L}}{Z_{u,u+L}^{u,L}} + \sum_{k < i} \sum_{l > j} p_{kl}^{u,L} \Xi_{ij,kl}^{u,L} \\ &= \frac{Z_{u,i-1} \widehat{Z}_{i,j} Z_{j+1,u+L}}{Z_{u,u+L}} + \sum_{k < i} \sum_{l > j} p_{kl}^{u,L} \Xi_{ij,kl} \,. \end{split}$$

Robust local structures

Average probability of an (i, j) pair over all folding windows containing the sequence interval [i, j]

$$\pi_{ij}^{L} = \frac{1}{L - (j - i) + 1} \sum_{u=j-L}^{i} p_{ij}^{u,L}$$

Direct Recursion:





Local structures (L=100) in a 740 nt region of human X chromosome

Cofold: How to deal with Concentration?

- Algorithmically that same as linear folding special energy contribution for "loop with the cut"
- Additional energy contribution for forming duplex
- At least 5 molecular species need to be taken into account (Dmitrov & Zuker, 2005): A, B, A₂, B₂, AB.
- Their folding energies and partition functions are easily computed

Cofold



Dot plot (left) and mfe structure representation (right) of the cofolding structure of the two RNA molecules AUGAAGAUGA (red) and CUGUCUUGAGACA.

Cofold: Concentration dependencies

$$Q = V^{n} \frac{a!b! \times (Z'^{A})^{n_{A}} (Z'^{AA})^{n_{AA}} (Z'^{AB})^{n_{AB}} (Z'^{BB})^{n_{BB}} (Z'^{B})^{n_{B}}}{n_{A}! n_{B}! 2 n_{AA}! 2 n_{BB}! n_{AB}!}$$

where $a = n_A + 2n_{AA} + n_{AB}$. The system minimizes the free energy $-kT \ln Q$. solving this optimization problem yields the equilibria: $[AA] = K_{AA} [A]^2$, $[BB] = K_{BB} [B]^2$. $[AB] = K_{AB} [A] [B]$. with $[A] = 6.023 \times 10^{23} n_A$, etc., and

$$\begin{split} & \mathcal{K}_{AA} = \frac{Z'^{AA}}{(Z^{A})^{2}} = \frac{(Z^{AA} - (Z^{A})^{2})e^{-\Theta_{I}/RT}/2}{(Z_{A})^{2}} = \frac{1}{2} e^{-\Theta_{I}/RT} \left(\frac{Z^{AA}}{(Z^{A})^{2}} - 1\right) \\ & \mathcal{K}_{BB} = \frac{1}{2} e^{-\Theta_{I}/RT} \left(\frac{Z^{BB}}{(Z^{B})^{2}} - 1\right) \\ & \mathcal{K}_{AB} = e^{-\Theta_{I}/RT} \left(\frac{Z^{AB}}{Z^{A}Z^{B}} - 1\right) \end{split}$$



Example for the concentration dependency for two mRNA-siRNA binding experiments.

RNAup: Small RNAs Binding to Large Ones

- RNA folding excludes pseudoknots, i.e., non outerplanar graphs
- cofold thus does not allow small RNA binding into loop regions of large ones
- ... but this happens in reality

Remedy: Compute energy/partition function



that subsequence [i, j] is unpaired and the energy of binding a short molecule in this location

RNAup

RNAup: Interaction part

$$Z^{I}[i,j,i^{*},j^{*}] = \sum_{\substack{i < k < j \\ i^{*} > k^{*} > j^{*}}} Z^{I}[i,k,i^{*},k^{*}]e^{-\beta I(k,k^{*};j,j^{*})}$$

$$Z^{*}[i,j] = P_{u}[i,j] \sum_{i^{*} > j^{*}} Z^{I}[i,j,i^{*},j^{*}];$$

$$P^{*}[i,j] = Z^{*}[i,j] / \sum_{k < l} Z^{*}[k,l]$$

RNAup: Application

Binding of siRNAs to VR mRNA.

 $P_u[i, i]$ (dashed line), P_i^* (thick black line), ΔG_i (thick red line). Below: activity of siRNA

Alternative Approach

Consider RNA Folding as a Machine Learning Problem Context Free Grammar + probabilities for production rules \Rightarrow Stochastic Context Free Grammars see work by Sean Eddy, Jotun Hein, and collaborators

Folding Kinetics

RNA molecules may have kinetic traps which prevent them from reaching equilibrium within the lifetime of the molecule. Long molecules are often trapped in such meta-stable states during transcription. Possible solutions are

- Stochastic folding simulations can predict folding pathways and final structures. Computationally expensive, few programs available.
- Predicting structures for growing fragments of the sequence can show whether large scale re-folding will occur during transcription. Cheap but inaccurate.
- Analysis of the energy landscape based on complete suboptimal folding can identify possible traps (local minima).

Kinetic Folding Algorithm

Simulate folding kinetics by a Monte-Carlo type algorithm: • - Generate all neighbors using the move-set Assign rates to each move, e.g.

$$P_i = \min\left\{1, \exp\left(-\frac{\Delta E}{kT}\right)\right\}$$

Select a move with probability proportional to its rate Advance clock $1/\sum_i P_i$.
Characterization of Landscapes

A landscape consists of a configuration space V, a move set within that configuration space and an energy function $f : V \to \mathbb{R}$. Simplest move set for secondary structure: opening and closing of base pairs.

Speed of optimization depends on the *roughness* of the Landscape. Measures of roughness suggested in the literature:

- Number of local optima
- Correlation lengths (e.g. along a random walk)
- Lengths of adaptive walks
- Folding temperature vs. glass temperature T_f/T_g
- Energy barriers between the local optima. Especially, the maximum barrier height ("depth" in SA literature)

Energy barriers

$$E[s, w] = \min \left\{ \max \left[f(z) | z \in \mathbf{p} \right] \, \middle| \, \mathbf{p} : \text{path from } s \text{ to } w \right\},$$
$$B(s) = \min \left\{ E[s, w] - f(s) \middle| w : f(w) < f(s) \right\}$$

Depth and Difficulty (borrowed from simulated annealing theory)

$$D = \max \left\{ B(s) \middle| s \text{ is not a global minimum} \right\}$$
$$\psi = \max \left\{ \frac{B(s)}{f(s) - f(\min)} \middle| s \text{ is not a global minimum} \right\}$$

Energy Barriers and Barrier Trees

Some topological definitions: A structure is a

- local minimum if its energy is lower than the energy of all neighbors
- local maximum if its energy is higher than the energy of all neighbors
- saddle point if there are at least two local minima that can be reached by a downhill walk starting at this point



Calculating barrier trees



The flooding algorithm:

Read conformations in energy sorted order.

For each confirmation x we have three cases:

- (a) x is a local minimum if it has no neighbors we've already seen
- (b) x belongs to basin B(s), if all known neighbors belong to B(s)
- (c) if x has neighbors in several basins B(s₁)...B(s_k) then it's a saddle point that merges these basins.
 Basins B(s₁),...,B(s_k) are then united and are assigned to the deepest of local minimum.

Information from the Barrier Trees

- Local minima
- Saddle points
- Barrier heights
- Gradient basins
- Partition functions and free energies of (gradient) basins
- Depth and Difficulty of the landscape

N.B.: A *gradient basin* is the set of all initial points from which a gradient walk (steepest descent) ends in the same local minimum.

Energy Landscape of a Toy Sequence



Folding Kinetics

Transition rates from x to y:

$$r_{yx} = r_0 e^{-\frac{E_{yx}^{-} - E(x)}{RT}} \text{ for } x \neq y$$

$$r_{xx} = -\sum_{y \neq x} r_{yx}$$

Kinetics as a Markov process:

$$\frac{\mathrm{d}\boldsymbol{p}_{x}}{\mathrm{d}t} = \sum_{y \in X} r_{xy} p_{y}(t) \, .$$

Transition states:

$$E_{yx}^{\neq} = \max\{E(x), E(y)\}$$

or more complex models (Tacker et al 1994, Schmitz et al 1996)

Reduced Description of the Folding Dynamics

Macrostates = Classes of a partition of the state space. Partition function for a macro state:

$$Z_{lpha} = \sum_{x \in lpha} \exp(-E(x)/RT)$$

Free energy of a macro state:

$$G(\alpha) = -RT \ln Z_{\alpha}$$

$$r_{\beta\alpha} = \sum_{y \in \beta} \sum_{x \in \alpha} r_{yx} \operatorname{Prob}[x|\alpha] \quad \text{for } \alpha \neq \beta$$
$$= \frac{1}{Z_{\alpha}} \sum_{y \in \beta} \sum_{x \in \alpha} r_{yx} e^{-E(x)/RT}$$

 $r_{\beta\alpha}$ "on flight" while executing the barriers program. Transition state free energy:

$$G_{\beta\alpha}^{\neq} = -RT \ln \sum_{y \in \beta} \sum_{x \in \alpha} e^{-\frac{E_{xy}^{\neq}}{RT}}$$









Refolding of a tRNA molecule.

Summary I:

. . .

- RNA structures can be computed efficiently by means of dynamic programming
- Computations are based on a set of carefully measures energy parameters and an additive energy model
- Algorithms exist for ground state energy and structure, full partition functions, density of states, interacting structures,
- The folding kinetics of a given RNA Sequence can also be investigated as the level of secondary structures
- VIENNA RNA PACKAGE

PART II: How Do RNAs Evolve

Basic Assumption

Selection Acts on Secondary Structures, Mutations acts on the underlying sequences \Rightarrow We need to understand the sequence-to-structure map of RNAs (hang on, we'll discuss the empirical evidence for that a bit later)

Sewall Wright's Fitness Landscapes



How do realistic fitness landscapes look like?

The RNA case is a special case of a very general paradigm:

 $genotype \mapsto phenotype \mapsto fitness$

What is the relationship between Genotyp and Phenotype? Central topic in any theory of evolution

because:

* Selection acts on the Phenotype

* Mutation/Recombination acts on the Genotype *Biopolymers* as the simplest model:

The molecule is **both** genotype (sequence) and phenotype (structure).

The map from genotype to genotype is determined by physical chemistry:

 \iff folding problem

Computational Analysis of the RNA Map

There are many more sequences than structures.

(.)-string: 3-letters (with constraints)

 \implies less than 3^n structures

but 4ⁿ sequences.

\implies Redundancy

How are sequences folding into the same structure distributed in sequence space?

Neutral Set $S(\psi) = \{x \in \mathcal{Q}_{\alpha}^{n} | f(x) = \psi\}$

Sensitivity and Neutrality



Distribution of structure distances

The Random Graph Model

Approach: Model $S(\psi)$ as a random induced subgraph Γ with a given value

$$\lambda = \frac{\langle \# \text{neutral neighbors} \rangle}{(\alpha - 1)n}$$

Threshold value:

$$\lambda^* = 1 - \left(\frac{1}{\alpha}\right)^{\frac{1}{\alpha - 1}}$$

Theorem. [Reidys, Stadler, Schuster] If $\lambda > \lambda^*$ then Γ is *a.s.* dense and connected, if $\lambda < \lambda^*$ then Γ is *a.s.* neither dense nor connected

A complication: Base Pairing Rules

Unpaired bases:

Alphabet $\mathcal{A} = \{A, U, G, C\}$ Paired bases: 5' and 3' side correlated:

Alphabet: $\mathcal{B} = \{AU, UA, GC, CG, GU, UG, \}.$

Thus consider only the set of compatible sequences $C(\psi)$: $S(\psi) \subseteq C(\psi) \equiv \mathcal{Q}_4^{n_u} \times \mathcal{Q}_6^{n_p}$.

 \implies Two neutrality parameters λ_u and λ_p

Connected Components of Neutral Networks



green 2 equal sized components yellow 3 components size 2:1

blue 4 equal sized components

gray

Explanation: for this deviation from the random graph model in terms of the energy model. Some structures can

be made only with a significant bias in the G/C ratio.



Closest Approach

Intersection Theorem. For any two secondary structures $\phi,$ and ψ holds

 $\mathcal{C}(\phi) \cap \mathcal{C}(\psi) \neq \emptyset$

What is the distance of neutral networks

$$\delta(\phi,\psi) = \min\{d(x,y)|f(x) = \phi \text{ and } f(y) = \psi\}$$

Random graph Theory: If $\lambda > \lambda^*$ then $\delta(\phi, \psi) \approx 2$. Computer simulations: upper bounds on $\delta(\phi, \psi)$:

n	GC	AU	AUGC
50	5.6	2.6	2.1
70	9.3	4.6	3.4
100	13.0	7.8	5.6

Accessibility

Fontana & Schuster 1998

Idea: The "interface" between two structures is large is they are "similar".

More precisely: Structure ψ is *accessible* for ϕ if $x \in S(\phi)$ is like to have neighbor (mutant) $x' \in S(\psi)$.

Structural characterization of "easy" (continuous) transitions:



SUMMARY: Sequence-Structure Map of RNA

- 1. Redundancy: Many more sequences than structures
- 2. *Sensitivity:* Small changes in the sequences may lead to large changes in the structure
- 3. *Neutrality:* A substantial fraction of mutations does not alter the structure.
- 4. Isotropy: $S(\psi)$ is "randomly" embedded in $C(\psi)$.

Implications:

- 1. Neutral Networks: $S(\psi)$ forms a connected "percolating" network in sequence space for all "common" structures.
- 2. *Shape Space Covering:* Almost all structures can be found in a relatively small neighborhood of almost every sequence.
- 3. *Mutual Accessibility:* The neutral networks of any two structures almost touch each other somewhere in sequence space.

Simulated Trajectories



Diffusion Constant

... can be deduced from Moran model:

$$D = \overline{\lambda} \frac{6Anp}{3+4Np} (1+1/N) \sim \begin{cases} (3/2)A(n/N) & p \gg 0 \\ 2Anp & p \ll 1 \end{cases} \quad \text{or } N \gg 1$$

 $\begin{array}{l} A \ \dots \ \text{replication rate} \\ n \ \dots \ \text{sequence length} \\ N \ \dots \ \text{population size} \\ p \ \dots \ \text{mutation rate} \\ \overline{\lambda} \ \dots \ \text{neutrality of network} \end{array}$

Dynamics of Interacting Replicators

$$\mathbb{I}_k + \mathbb{I}_j \longrightarrow \mathbb{I}_l + \mathbb{I}_k + \mathbb{I}_j$$

With mutation:

$$\dot{x}_k = x_k \left(\sum_j A_{kj} x_j - \sum_{i,j} A_{ij} x_i x_j \right) + \sum_{l,j} \left(Q_{kl} A_{lj} x_j x_l - Q_{lk} A_{kj} x_k x_j \right)$$

where

$$Q_{kl} = (1-p)^{n-d(k,l)} \left(\frac{p}{\alpha-1}\right)^{d(k,l)}$$

How does this behave in sequence space?



B.M.R. Stadler, Adv. Complex Syst. (2003)



Left: Diffusion coefficient *D* as a function of the mutation rate for N = 10, 20, 30, 40, 80 and n = 10, 20, 30, 40, 80 such that N/n = 1 after equilibration for 10^5 timesteps. Right: Dependence of the ratio D/p on N/n.

An RNA-Based Model in the Plane



Target hypercycle with 8 members.

Model:

Hypercyclically coupled species, each sequence has a *function* that depends on its structure.

Spatial Extension: CA Model



Rules of replication. For each of the neighbors (•) of the empty cell (marked by a bold outline) the replication rate ρ_z is computed taking into account their neighbors in the direction of the replication (°) as potential catalysts. The neighbor with the largest values of ρ_z invades the empty position. In this example, for the chosen replicator, only three of its neighbours are catalysts according to the hypercycle topology.



Spirals formed after 3000 generations in an evolution experiment started with 300 random sequences in the absence of parasites.

see also Borlijst & Hogeweg (1993)

Diffusion in Sequence Space



Summary

- Neutrality of the Sequence-Structure Map implies diffusion/drift-like motion in sequence independent of details of the selection/mutation mechanisms and whether spatial extension is taken into account or not.
- The basic assumption of molecular phylogenetics, namely a dominating influence of drift in sequence evolution, holds true even when phenotypic evolution is dominated by interactions

(co-evolution).

 TODO Development of a rigorous mathematical theory describing the motion in sequence space of a population with strong interactions.

Evolutionary histories of some structured RNAs

Ribosomal RNAs (rRNAs) are the most frequently used sequence data for reconstructing phylogenies from molecular data How does that work:

In a nutshell:

(1) compute evolutionary distances from the sequence data

(2) "fit" an additive tree to the distances

(In reality, there are other methods such as maximum parsimony and maximum likelihood approaches, but the basic idea is the same)

Observation: all tRNAs have more or less the same clover-leaf structure.

MicroRNAs

- processed from precursor hairpins
- short (~ 22nt) RNA molecules
- highly conserved

Function

- bind to 3'UTRs of mRNA targets
 - supress expression of this mRNA
 - mark mRNA molecule for degradation
 - in plants involved in DNA methylation



00001	THE REMOVEMENT DE DEQUERCE HERORALENT			
File: miR-223.ps Page 1 of 2	Date: Mon Oct 17 14:34:09 2005			
lre-miR-223	UGUCAGUUUGUCAAAUACCCC	2:		
ru-miR-223	UGUCAGUUUGUCAAAUACCCC	2:		
ga-miR-223	UGU <mark>C</mark> AGUUUGU <mark>C</mark> AAA <mark>U</mark> ACCCC	2:		
go-miR-223	UGU <mark>CA</mark> GUUUGU <mark>CAAA</mark> UACCCC	2:		
sa-miR-223	UGU <mark>CA</mark> GUUUGU <mark>CAAA</mark> U <mark>ACCCC</mark>	2:		
ml-miR-223	UGU <mark>C</mark> AGUUUGUCAAAUACCCC	2:		
mu-miR-223	UGUCAGUUUGUCAAAUACCCC	2:		
pa-miR-223	UGU <mark>CA</mark> GUUUGU <mark>CAAA</mark> U <mark>ACCCC</mark>	2:		
ruler	1			



MicroRNAs — processing and function



MicroRNAs ...

- transcribed in longer transcripts (primary-miRNA)
- in some cases: *polycistronic* "clusters"
- ► Drosha processing → precursor miRNA
- export to cytoplasm
 Exportin-5 pathway
- ► Dicer processing → mature miRNA
Evolution of microRNA Families: mir-17 clusters

Many miRNAs are transcribed from polycistronic transcripts Most spectacular example: Human **mir-17** clusters



J. Mol. Biol. 339: 327-335 (2004)

Case Study: mir-17 clusters



Structure of the pri-pre-mir-17 at the human X chromosome.

Construction of Gene Trees

from concatenated sequences in the cluster



Distant Homologies with unreliable Alignments

How to quantify sequence similarity when we cannot get a good alignment?

- measure pairwise sequence similarity s(x, y)
- compare to the distribution of similarity values of alignments of shuffled sequences
- define a z-score

$$z(x,y) = \frac{s(m,y) - \langle s(\pi(x),\pi'(y)) \rangle_{\pi,\pi'}}{\sqrt{\operatorname{var}_{\pi,\pi'}(s(\pi(x),\pi'(y)))}}$$

• use z(x, y) as similarity measure in WPGMA clustering

Gene Tree of mir-17 cluster members



Collapsed tree of microRNA subgroups



 obtained by collapsing vertebrate, insect, and nematode species trees to single vertices

 next step: combine gene trees and synteny information to a duplication history

Scenario for the evolution of the mir17 family ancestral mir17 cluster probably contained mir-17, mir-19 and mir-92





Scenario for the evolution of the mir17 family first detectable duplication event: branch mir-17 and mir-18



Scenario for the evolution of the mir17 family series of duplications: branch mir-19 and mir19b, mir-17 and mir-93



Scenario for the evolution of the mir17 family genome wide duplication:

duplication of whole cluster and loss of individual miRNAs



Scenario for the evolution of the mir17 family independent miRNA duplications in type I cluster



Scenario for the evolution of the mir17 family split of teleosts and mammalia teleost specific genome duplication



Scenario for the evolution of the mir17 family split of teleosts and mammalia teleost specific genome duplication



History of the mir-17 cluster: updated data



Further Examples: let-7 family



Further Examples: *mir-1* and *mir-30*



Further Examples: mir-9, mir-23, mir130/301







mir-130 cluster

Expansion of the Metazoan MicroRNA Repertoire



Similar Situation: snoRNA

- snoRNAs direct chemical modification of other RNAs (mostly rRNA, snRNA, and (some?) messenger RNAs
- ▶ two classes: box-H/ACA and box-C/D
- known in eukaryotes and archea, not in eubacteria

H/ACA box snoRNAs in Vertebrates



Vertebrate Y RNAs



Outgroup

Summary

- The genotype-phenotype map of RNA is charcterized by an interplay of "ruggedness" and neutrality
- Selection plus drift results in diffusion on neutral networks
- Many non-coding RNAs have highly constrained (i.e., evolutionarily very well conserved) structures but fairly rapidly evolving sequences
- Drift of sequences is independent of the details of the selection mechanism
- Ongoing research: elucidate the evolutionary histories of structured ncRNAs

PART III: The Modern RNA World



Multiple Origins of ncRNAs



Surveys for noncoding RNAs

- ► > 5% of the human genome is under stabilizing selection (from man/mouse comparison), less than 1/3 of this codes for protein
- Virtually the entire genome is transcribed as primary nuclear transcripts in at least one direction (ENCODE Genes&Transcripts group, unpublished data)
- ► ~ 80% of the ENCODE regions are transcribed in as parts of protein coding transcripts including introns and UTRs
- Only a tiny part of the primary transcripts is protein coding
- Large fraction of apparently non-protein-coding cDNAs
- The functions of most of these transcripts are unclear.

"There is need for reliable experimental and computational methods for comprehensive identification of non-coding RNAs."

-International Human Genome Sequencing Consortium, Nature 431, p.943, October 2004

The ENCODE Project



ENCyclopedia Of DNA Elements

- ▶ Public research consortium launched by NHGRI in 2003
- Purpose: "testing and comparing existing methods to rigorously analyze a defined portion of the human genome sequence".
- <u>Focus:</u> specified 30 megabases (1% of genome) in more than 20 species
- Informally organized in subgroups: Sequencing Technology, Comparative Genomics, Genes and Transcripts, Genetic Variation, ...
- Results from 1st phase currently under review
- Phase 2: scale-up to complete genome

(Data presented by Tom Gingeras in Bethesda, Jan 12 2006)

- Only a fraction of processed RNA transcripts correspond to GeneCode annotated transcripts: 70% correlated with annotated (m)RNAs 52% correlate with annotated protein coding sequences
- Substantial fraction of transcription is specific of cellular conditions

only 2.6% of transfrags are common to all 11 cell-lines.

- The same genomic sequence may be processed into multiple RNA sequences with different fates
- Virtually the entire genome is transcribed as primary nuclear transcript in at least one direction.

Transcriptional output is MUCH more extensive AND much more complex than previously thought.

Recall: Sequence-Structure Map of RNA

- 1. Redundancy: Many more sequences than structures
- 2. *Sensitivity:* Small changes in the sequences may lead to large changes in the structure
- 3. *Neutrality:* A substantial fraction of mutations does not alter the structure.
- 4. Isotropy: $S(\psi)$ is "randomly" embedded in $C(\psi)$.

Implications:

- 1. Neutral Networks: $S(\psi)$ forms a connected "percolating" network in sequence space for all "common" structures.
- 2. *Shape Space Covering:* Almost all structures can be found in a relatively small neighborhood of almost every sequence.
- 3. *Mutual Accessibility:* The neutral networks of any two structures almost touch each other somewhere in sequence space.

Proc.Roy.Soc.B 255 279-284 (1994), Proc. Natl. Acad. Sci. USA 93, 397-401 (1996),

Bull. Math. Biol. 59, 339-397 (1997), RNA 7: 254-265 (2000).



Nucl. Acids Res. 26: 3825-3836 (1998), Comp. & Chem. 23: 401-414 (1999)

Examples: HIV-1 TAR-hairpin



Flaviviridae: Nucl. Acids Res. 29: 5079-5089 (2001), Picornaviridae: J. Gen. Virol. 85: 1113-1124 (2004), Broad survey: Bioinformatics 20: 1495-1499 (2004)

Examples: Picornaviridae: Cis-acting-Replication Element (CRE)

The function of the CRE probably involves the initiation of the synthesis of the negative-sense strand template RNA during virus replication.



predicted in Nucl. Acids Res. 29 5079-5089 (2001),

experimentally detected by Gerber, Wimmer Paul J. Virol. 75 10979-10990 (2001).

A Method for Large Genomes: RNAz

 \ast Two ingredients: Thermodynamic Stability & Structure Conservation

Measuring thermodynamic stability of ncRNAs

- Naturally occurring structured RNAs have a lower folding energy compared to random sequences of the same size and base composition?
 - 1. Calculate native MFE m.
 - 2. Calculate mean μ and standard deviation σ of MFEs of a large number of shuffled random sequences.
 - 3. Express significance in standard deviations from the mean as *z*-score

$$z = \frac{m - \mu}{\sigma}$$

 Negative z-scores indicate that the native RNA is more stable than the random RNAs.

Efficient calculation of stability z-scores

The mean μ and standard deviation σ of random samples of a given sequence are functions of the length and the base composition:

$$\mu, \sigma(length, \frac{GC}{AT}, \frac{G}{C}, \frac{A}{T})$$

- **Calculating** *z*-scores is thus a 5 dimensional regression problem.
- The regression problem is solved using a Support Vector Machine regression algorithm.
- The SVM was trained on 10,000 synthetic sequences spaced evenly in the variable space.
- The regression calculation is of the same accuracy as the sampling procedure.



z-scores of known ncRNAs

ncRNA Type	No. of Seqs.	Mean z-score
tRNA	579	-1.84
5S rRNA	606	-1.62
Hammerhead ribozyme III	251	-3.08
Group II catalytic intron	116	-3.88
SRP RNA	73	-3.37
U5 spliceosomal RNA	199	-2.73

- Functional RNAs are clearly more stable than random sequences.
- However: The scores are too small to discriminate reliably in a genome-wide screens since the z-score distributions have heavy tails.

Consensus folding using RNAalifold

- RNAalifold uses the same algorithms and energy parameters as RNAfold
- Energy contributions of the single sequences are averaged
- Covariance information (e.g. compensatory mutations) is incorporated in the energy model.
- It calculates a consensus MFE consisting of an energy term and a covariance term:

The structure conservation index



 The SCI is an efficient and convenient measure for secondary structure conservation.
Separation of native ncRNAs from random controls in two dimensions



z-score

Classification based on both scores



Classification based on both scores



Implementation and availability

- ► The approach is implemented in ANSI C in the program RNAz.
- ▶ The *z*-score regression is limited to 400 nucleotides.
- The classification model is currently limited to alignments of six sequences.
- At least an order of magnitude faster than other programs.
- RNAz is freely available: Download from www.tbi.univie.ac.at/~wash/RNAz

Proc. Natl. Acad. Sci. USA 102: 2454-2459 (2005)

Screening the human genome

Large scale comparative screen including:

- human, mouse, rat, dog
- chicken
- fugu, zebrafish
- Reduction of the \approx 3.095 MB human genome:
 - \blacktriangleright Take \approx 5% of the best conserved regions
 - Remove all annotated coding exons
 - Only take alignments strictly conserved in all 4 mammals.
- \blacktriangleright \rightarrow 438,788 alignments alignments covering 82.64 MB





Results of Human Genome Screen

	Genome Coverage		Alignments	RNAz hits $p > 0.9$		
	Size	Fraction	Number	Size	Fraction of	Number
	(MB)	(%)		(MB)	input (%)	
Human genome	3,095.02	100.00	-			
PhastCons most conserved	137.85	4.81	1,601,903			
without coding regions	110.04	3.84	1,291,385			
without alignments $< 50 nt$	103.83	3.33	564,455			
Set 1: 4 Mammals	82.64	2.88	438,788	5.46	6.62	35,985
Set 2: + Chicken	24.00	0.85	104,266	1.34	5.50	8,802
Set 3: $+$ Fugu or zebrafish	6.86	0.24	30,896	0.14	2.03	996

Nature Biotechn. 23: 1383-1390 (2005)

Pictures instead of Numbers





Distribution related to known protein gene annotation



Sensitivity on known classes of ncRNAs



Not all ncRNAs have conserved secondary structures!



Other RNAz Screens

 Urochordates: Ciona intestinalis & Ciona savignyi only a few conserved RNA with Oikopleura dioica Bioinformatics 21(S2): i77-i78

 Nematodes: Caernorhabditis elegans & Caenorhabditis briggsae

JEZ:MDE 2006 epub

- Teleost fishes: Danio rerio, Takifugu rubripes, Tetraodon nigroviridis, Oryzias latipes (partial) (in progress)
- Trypanosomatids: Trypananosoma and Leishmania species
- Yeasts. (joint work with Kay Nieselt and Stephan Steigele)

Summary

Predicted structured RNAs (RNAz predictions, p > 0.9)



Novel Human ncRNA Candidates



Novel ncRNA Candidates in Caenorhabditis



Efforts to Annotate the RNAz Results

ongoing effort

- Large number of microRNA candidates
- approximately 30-40 good H/ACA-box snoRNAs
- only 6% of hits (comparable to estimated false positive rate) overlaps with predicted coding regions
- few clusters of signals with high sequence-similarity work in progress: structure-based clustering (joint work with Rolf Backofen's lab in Freiburg)

BOTTOM LINE: most signals still unclassified. We need MUCH better methods to recognize members of known RNA classes

RNAmicro: A classificator for microRNA Precursors

- Input: Multiple Sequence alignment
- Preprocessing: non-restrictive check for almost-hairpin structure

Some known microRNA precursors, notably some let-7 family members have small branches!

SVM Classification with few descriptors:

Property	#	Descriptors
Structure	2	Is, Ih
Sequence composition	1	G+C
Sequence conservation	4	S51, S31, S0, Smin
Thermodynamic stability	4	Ē, ē, ŋ, z
Structure conservation	1	Econs

ISMB 2006, in press

Results: Caenorhabditis



Results: Mammals



Clustering



Proof of Concept: tRNAs in Ciona intestinalis



Summary

- Some classes of ncRNAs, namely the structures ones, can be found efficiently by means of comparative genomics
- There are Tens of Thousands of structured RNAs of unknown function in the human genome
- Some of them probably act, like microRNA and snoRNAs by binding to other RNAs. These could be investigated using RNA cofolding approaches (ongoing research).
- So far, we know only of the proverbial tip of the iceberg of the complexity of cellular regulation
- ▶ & RNA bioinformatics is a really cool research topic ...

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