Print your name: __________________________________________________________

- If you need more space to answer a question than we give you, you may use the backs of pages or you may use additional sheets of paper and attach them to the exam. Make sure that we know where to look for your answer!

- Read each question carefully and make sure that you answer everything asked for. Write legibly so that we can read your solutions. Please do not write anything in red.

- We suggest that for solutions that require you to write Java code, you include comments. They will help your grader understand what you intend, which can help you get partial credit.

- Hand in only what you want graded. We do not want your scrap paper unless it contains solutions you want us to grade.

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Question 1 24 points

Short answer

(a) (4 points)
In the k-means program we initialized the color list with k unique colors from the picture. After the first clustering there were no empty clusters. Yet later empty clusters sometimes arise. Explain how this can happen.

(b) (4 points)
Describe an efficient way to implement a queue in an array.
(c) (4 points)
Describe the difference between an ADT and a data structure. Give an example of each.
How are they related?

(d) (4 points)
Abstract classes and interfaces are similar in many ways. What things are allowed in an
abstract class that are not allowed in an interface? What is the reason to have interfaces in
Java, when everything possible in an interface is possible in an abstract class?
(e) (4 points)
We have seen the Template design pattern. Explain this pattern and describe a class example where we used it.

(f) (4 points)
The Stack class in the Java library extends the Vector class. Vector is an earlier version of ArrayList with similar operations (e.g. get, add, contains, set, remove). The Stack class then implements the operations empty, peek, pop, and push. What principles of ADTs and Object-Oriented design does this violate? Why is this bad?
Question 2 16 points

Below is some code for a singly-linked (non-circular) list class that does not use a sentinel or dummy list head node. It does not have a tail reference or a current reference. The data stored in each node is an int. Note that in this representation, the last element in the list is indicated by having a next pointer of null. We will ask you to implement two methods for this class.

Here is the code:

```java
public class SimpleSLL {
    private Element head; // The first element of the list

    /**
     * A private class inner representing the elements in the list.
     */
    private class Element {
        public int data;
        public Element next;

        /**
         * Constructor for a linked list element, given an object.
         * @param obj the data stored in the element.
         */
        public Element(int theData) {
            data = theData;
            next = null;
        }
    }

    /**
     * Constructor to create an empty singly linked list.
     */
    public SLL() {
        head = null;
    }

    /**
     * Is this list empty?
     */
    public boolean isEmpty() {
        return (head == null);
    }

    // Other methods not shown
}
```
(a) (8 points)
Write a recursive method sum that, given a reference to an Element elt, will return the sum of data in the sublist whose head is referenced by elt. (Note that elt may refer to an Element in the middle of a list. In this case sum should return the sum of the data in the sub-list that starts at that Element and continues to the end of the list.) We define the sum of an empty list to be 0. Given this helper method we can write the sum the entire list by calling sum(head). (Partial credit for a non-recursive solution.)

public int sum(Element elt) {

(b) (8 points)
Write a method append that, given an int value, will append an Element containing value to the end of this list. Note that because you have no tail reference you must find the correct place to append.

public void append(int value) {
Question 3 15 points

Consider the following classes:

```java
class SuperClass {
    public void doIt() {
        doItMore();
        System.out.println("Super’s doIt");
    }

    public void doItMore() {
        System.out.println("Super’s doItMore");
    }

    public void doItSuper() {
        System.out.println("doItSuper");
    }
}

class SubClass extends SuperClass {
    public void doIt() {
        super.doIt();
        System.out.println("Sub’s doIt");
    }

    public void doItMore() {
        System.out.println("Sub’s doItMore");
        super.doItMore();
    }

    public void doItSub() {
        System.out.println("doItSub");
    }
}
```

Assume that the following declarations are in a method in another class:

```java
SuperClass superObj = new SuperClass();
SuperClass superObj2 = new SubClass();
SubClass subObj = new SubClass();
```
(a) (6 points)
For each of the following method calls, show what it would print or explain why the
method call is not legal.

superObj.doItSuper();

superObj.doItSub();

superObj2.doItSuper();

superObj2.doItSub();

subObj.doItSuper();

subObj.doItSub();

(b) (9 points)
Show the output from each of the following method calls:

superObj.doIt();

superObj2.doItMore();

subObj.doIt();
Question 4  16 points

Write a method `findNode(E value)` which finds a `BinaryTree` node whose element equals value in a heap-ordered binary tree. Assume that the type `E` implements `Comparable`, so that you can compare element values using `compareTo`. Write a recursive helper method.

A heap-ordered binary tree is a binary tree where the minimum value is at the root and a node's value is always smaller than its children's values. Note that this fact can under some circumstances let us avoid searching in a subtree. For full credit your method should take advantage of this and not search in subtrees that could not possibly contain a node whose data equals value. (Note that the data is stored in a binary tree. We can have the heap order property without storing the values in an array or an arraylist.)

```java
/**
 * Searches for an element in this heap-ordered binary tree.
 * @param value the element value to search for.
 * @return a BinaryTree node who's data equals value, or null if
 * no such node exists in this subtree
 */
public BinaryTree<E> findNode(E value) {
```
Question 5 14 points

(a) (6 points)
The TreeMap get method takes $\Theta(\log n)$ time on average. You do a timing test and discover that performing 10,000 get operations on a map whose size is 1,000 takes 0.01 seconds. How long would you expect 20,000 get operations on a map whose size is 4,000,000 to take? (You may use the approximations $\log 1000 = 10$ and $\log 4,000,000 = 22$.)
(b) (8 points)
Below is the RubberLines class, which we saw in class. The idea is that when the user presses the mouse one end of a segment is anchored there, and as long as the mouse is being dragged the other end follows the mouse. Add code to init to set up listeners and complete the mousePressed and mouseDragged methods to make this happen.

```java
public class RubberLines extends JApplet implements MouseListener, MouseMotionListener {

private Point point1 = null;
private Point point2 = null;

public void init() {
    // *** Fill in code to set up listeners ***

    // Other code not shown (and need not be written by you!)
}

public void mousePressed(MouseEvent event) {
    // *** Fill in the body of this method ***
}

public void mouseDragged(MouseEvent event) {
    // *** Fill in the body of this method ***
}

private class Canvas extends JPanel {
    public void paintComponent(Graphics page) {
        super.paintComponent(page);
        if (point1 != null && point2 != null)
            page.drawLine(point1.x, point1.y, point2.x, point2.y);
    }
}
```

Question 6 15 points

In SA-9 you wrote the class StateAndCities, which used a Map. In this map, the keys were names of states and the associated value for a key was a Set of names of cities that are within the state. Part of this class is shown below:

```java
public class StatesAndCities {
    private Map<String, Set<String>> stateCityMap;

    /** *
     * Constructs empty map *
     */
    public StatesAndCities() {
        stateCityMap = new TreeMap<String, Set<String>>();
    }

    /** *
     * Adds a state/city pair to the atlas.
     * @param state the state to add to
     * @param city the city to add
     */
    public void addPair(String state, String city) {
        // Code not shown
    }

    /** *
     * Is the city is associated with the state in the map
     * @param state the state to look for
     * @param city the city to look for
     * @return true if city is in state
     */
    public boolean isCityInState(String state, String city) {
        // Code not shown
    }
}
```

You are to add a method getStatesContainingCity to this class which, given the name of a city, returns a set of all states that contain a city with this name. (If none contain the city name, it returns the empty set.) Thus, if the current state of the map were:

- MA: Boston  Concord
- NH: Concord  Hanover
- TN: Nashville

A call to getStatesContainingCity("Concord") should return the set {MA, NH}. You may use any of the methods given above if they are useful. The method is started on the next page.
/**
 * Returns a Set containing the names of all states in the
 * stateCityMap whose associated Set contains the named city.
 * @param city the city that we seek
 * @return a set of states that contain city
 */
public Set<String> getStatesContainingCity(String city) {